

# Time change and Universality in Turbulence

Ole E. Barndorff-Nielsen and Jürgen Schmiegel

*Thiele Centre for Applied Mathematics in Natural Science,  
Aarhus University,  
DK-8000 Aarhus, Denmark*

## Abstract

We discuss a unifying description of the probability densities of turbulent velocity increments for a large number of turbulent data sets that include data from low temperature gaseous helium jet experiments, a wind tunnel experiment, an atmospheric boundary layer experiment and a free air jet experiment. Taylor Reynolds numbers range from  $R_\lambda = 80$  for the wind tunnel experiment up to  $R_\lambda = 17000$  for the atmospheric boundary layer experiment. Empirical findings strongly support the appropriateness of normal inverse Gaussian distributions for a parsimonious and universal description of the probability densities of turbulent velocity increments. Furthermore, the application of a time change in terms of the scale parameter  $\delta$  of the normal inverse Gaussian distribution results in a collapse of the densities of velocity increments onto Reynolds number independent distributions. We discuss this kind of universality in terms of a stochastic equivalence class that reformulates and extends the concept of Generalized Extended Self-Similarity.